



McGill

COSMO – *Stochastic Mine Planning Laboratory*
Department of Mining and Materials Engineering

Stochastic Mine Planning Concepts,
Applications and Contributions:
From past developments to production
scheduling with ‘future data’

Roussos Dimitrakopoulos

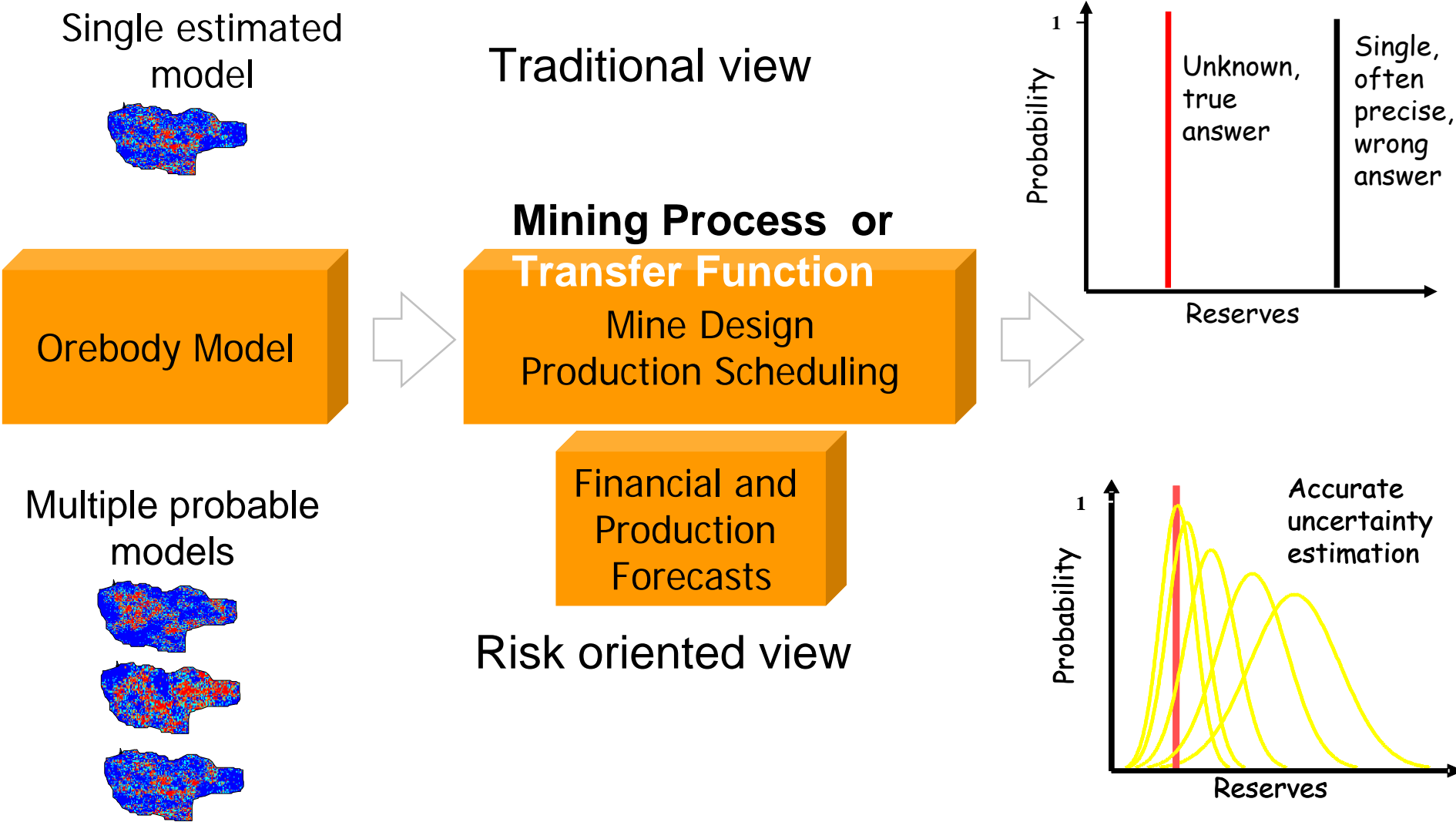
Overview

- The economic side of uncertainty
- Models of geological uncertainty
- Limits of traditional mine design optimization
- Shifting the paradigm: Stochastic mine planning
- Using uncertainty to improve project performance
- Uncertainty is great!

Risk in Mining: A World Bank Survey

- 60% of mines had an average rate of production LESS THAN 70% of planned rate
- In the first year after start up, 70% of mills or concentrators had an average rate of production LESS THAN 70% of design capacity
- Key contributor to mining risk felt in all downstream phases:
Geology and reserves

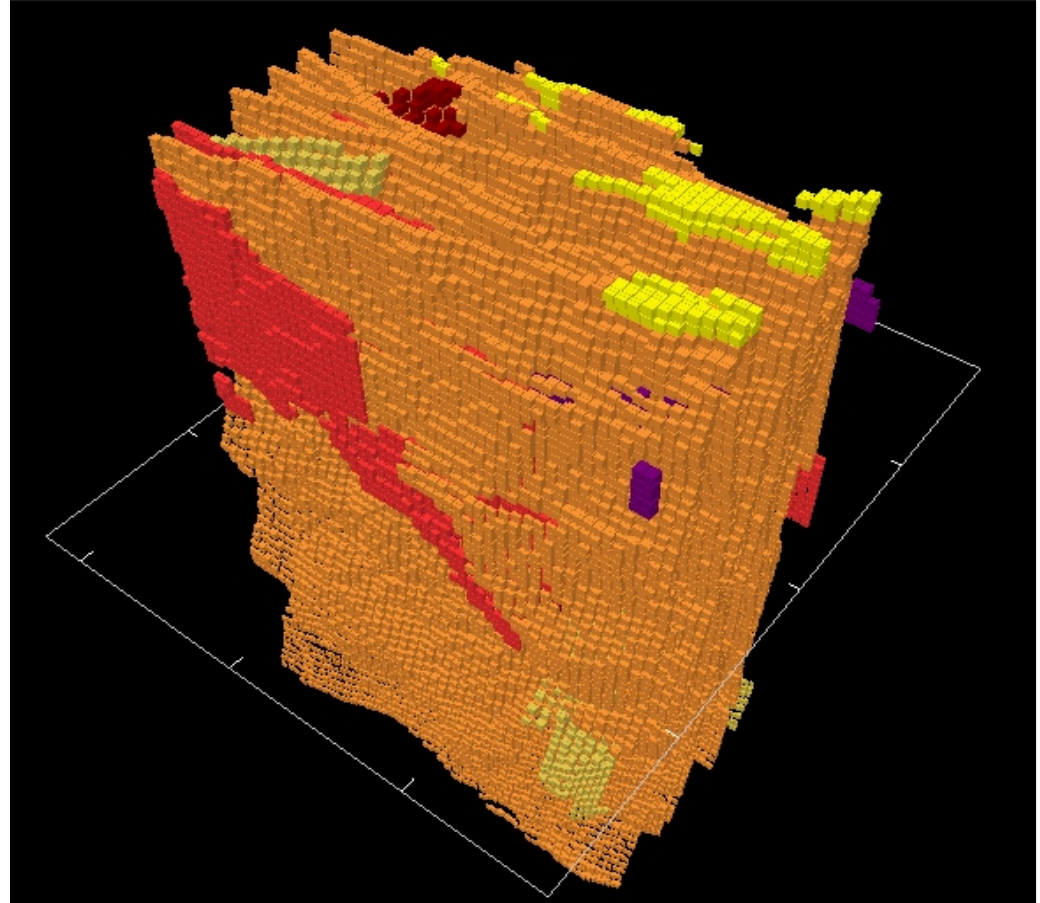
Mining Project Valuation



Quantitative Models of Geological Uncertainty:

Stochastic or geostatistical
conditional simulations

Describing the Uncertainty about a Gold Deposit



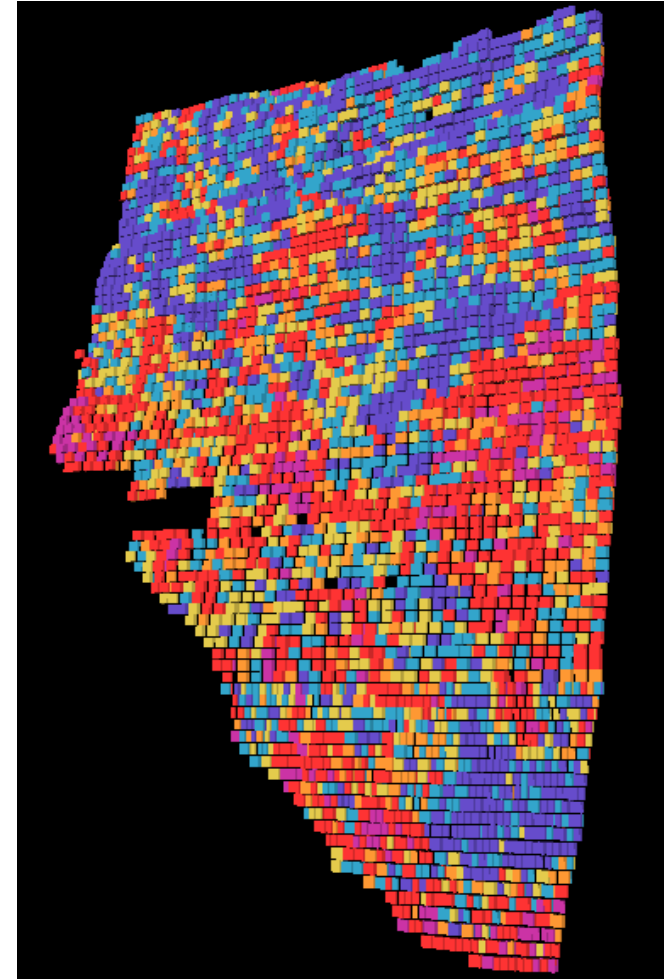
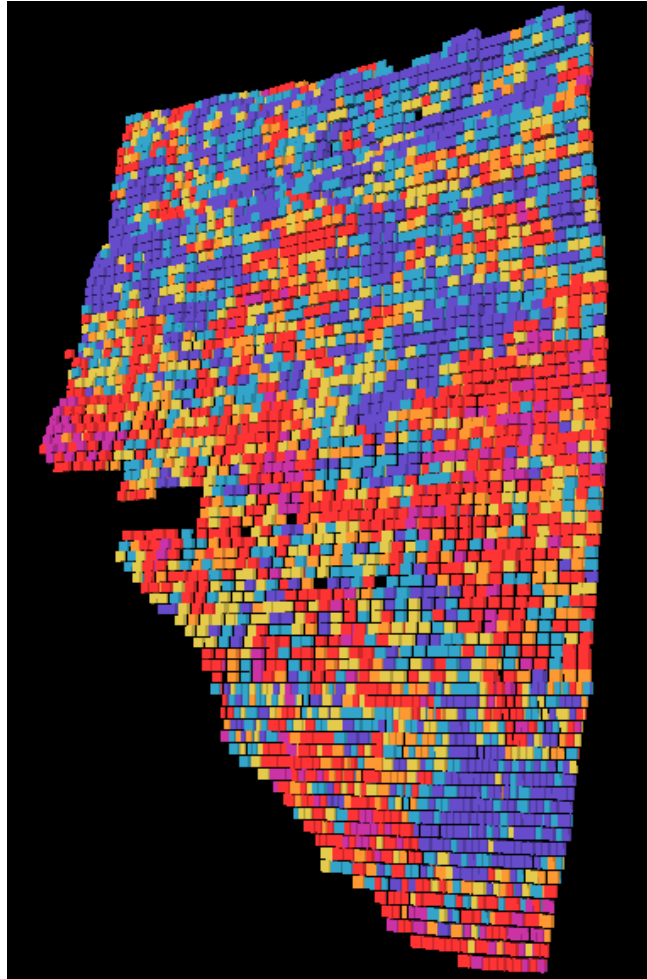
Model characteristics:

- o Large number of blocks
- o Multiple domains
- o Resource classes with specific sample selection criteria

A gold load

Loco Describing the Uncertainty about a Gold Deposit

Simulation #1



Uncertainty is not a “Bad Thing”

Many managers believe that uncertainty is a problem and should be avoided.....

... you can take advantage of uncertainty. Your **strategic investments will be sheltered** from its adverse effects while remaining exposed to its upside potential. Uncertainty will create opportunities and value.

Once your way of thinking explicitly includes uncertainty, **the whole decision-making framework changes.**

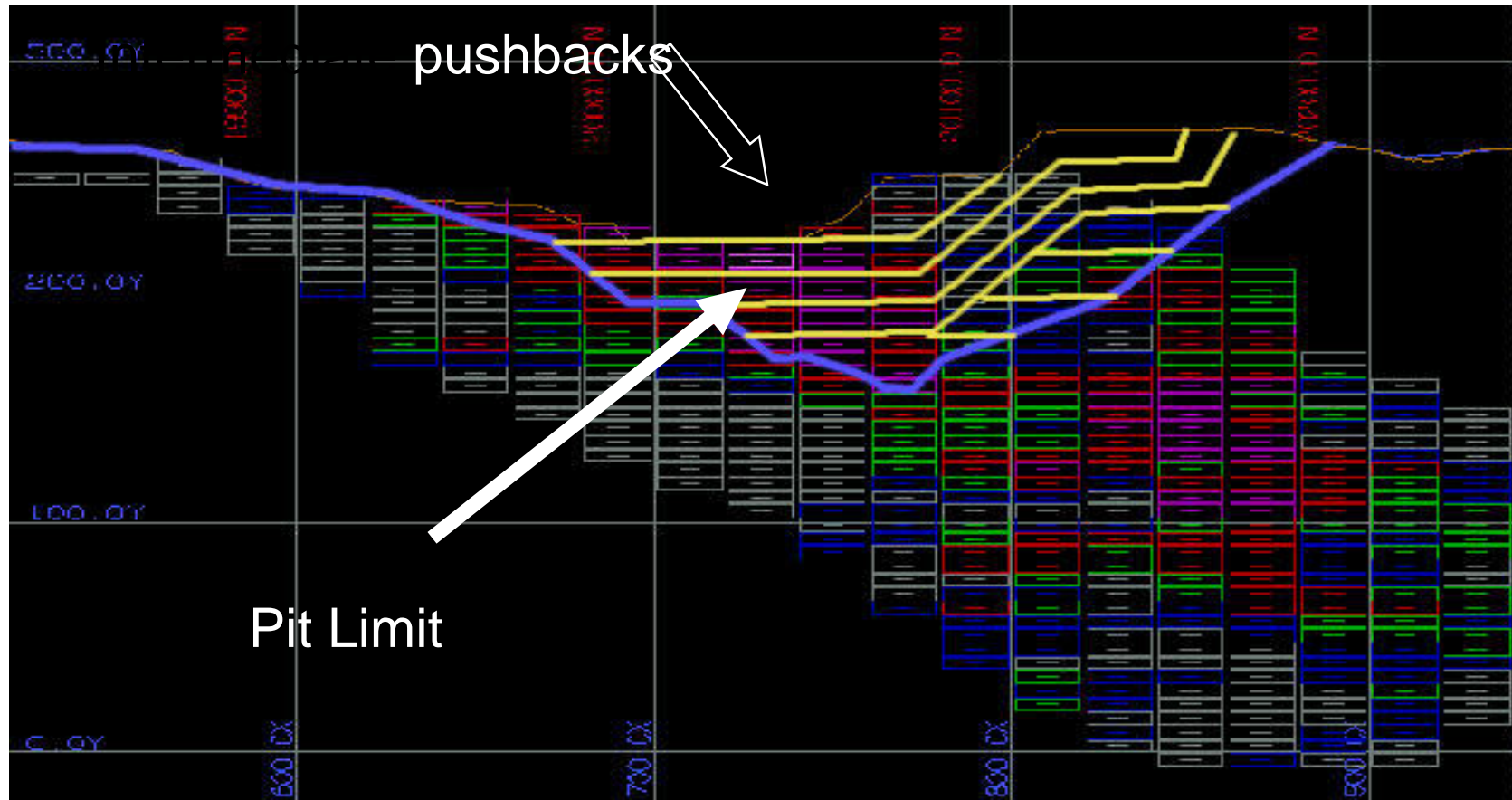
Martha Amram and Nalin Kulatilaka
in “Real Options”

Moving Forward in Optimization

Limits of traditional mine design

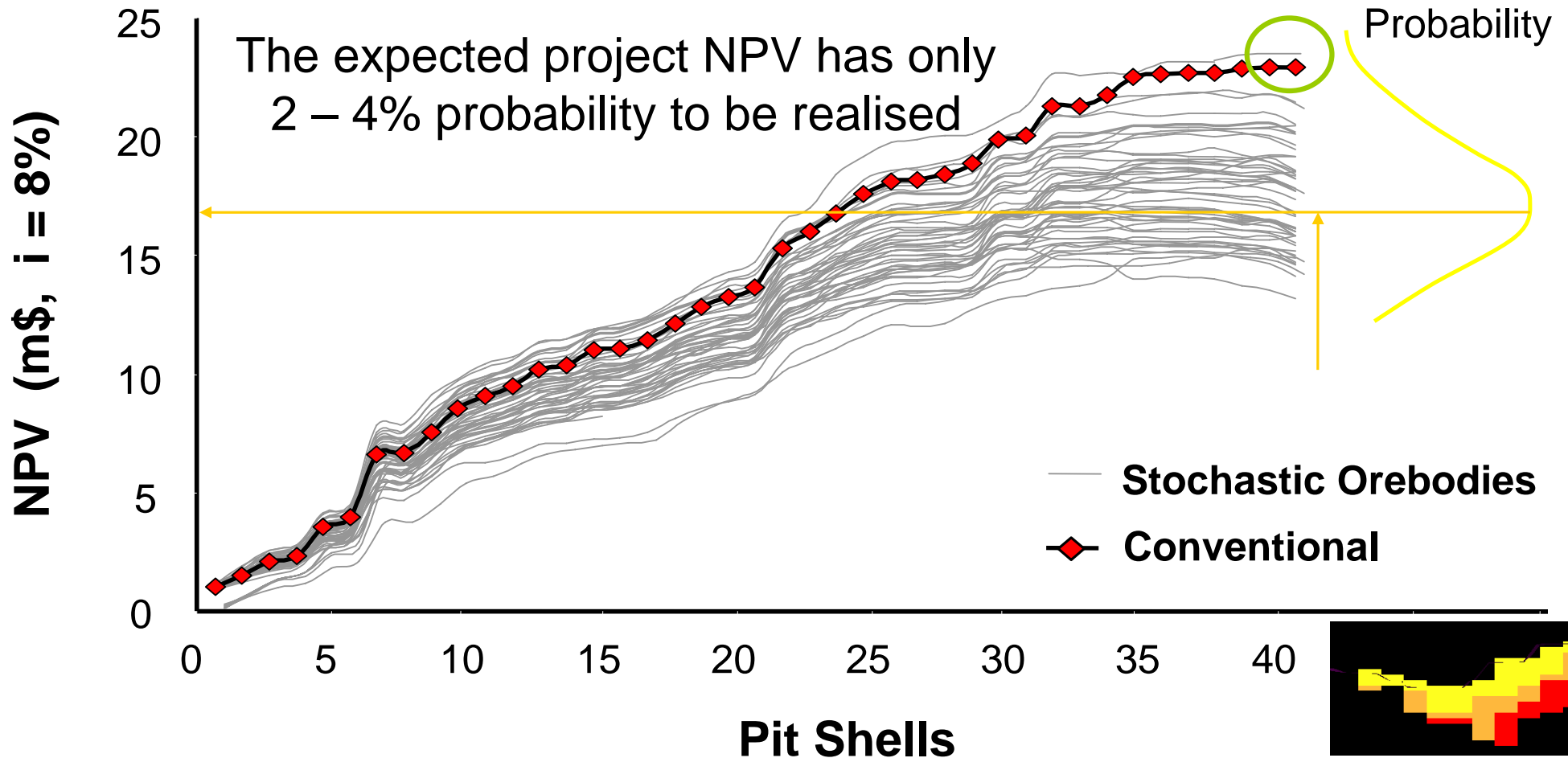
Using models of uncertainty

Open Pit Mine Design and Production Scheduling



Risk Analysis in a Mine Design


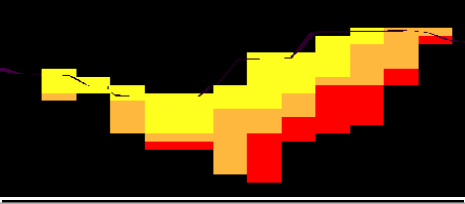

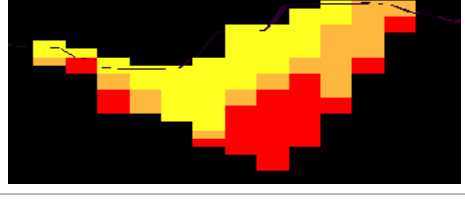
Limits of Traditional Modelling



Moving Forward Step 1

Exploring existing technologies

Past Work – Open Pit Mine Design

Pit Design	Upside Potential (m\$)			Downside Potential (m\$)		
	CB-1	CB-2	CB-3	CB-1	CB-2	CB-3
	2.3	2.41	1.8	0.0	-0.079	-0.20
	1.3	2.1	1.6	-0.78	-0.15	-0.51
	2.4	2.43	1.9	0.0	-0.022	-0.28
	2.9	2.40	1.2	0.0	-0.16	-0.96

Moving Forward Step 2

Re-writing optimizers

Models of Uncertainty in Optimization

Integer Programming

An objective function

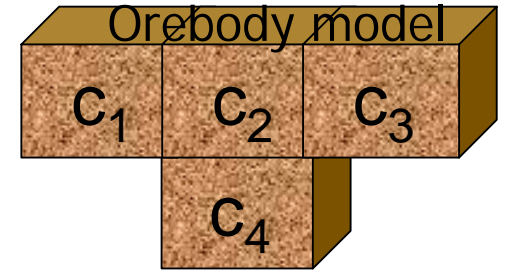
Maximise $(c_1x_1^1+c_2x_2^1+\dots)$...

Subject to

$$c_1x_1^1+c_2x_2^1+\dots \geq b_1$$



$$c_1x_1^p+c_2x_2^p+\dots \geq b_p$$



c = constant

x_1^1 = binary variable

→ Period 1

→ Period p

Stochastic Integer Programming

The objective function now

Maximise $(s_{11}x_1^1 + s_{21}x_2^1 + \dots + s_{12}x_1^1 + s_{22}x_2^1 + \dots)$

Subject to

$$s_{11}x_1^1 + s_{21}x_2^1 + \dots \geq b_1$$



$$s_{11}x_1^p + s_{21}x_2^p + \dots \geq b_1$$

$$s_{12}x_1^p + s_{22}x_2^p + \dots \geq b_1$$

$$s_{1r}x_1^p + s_{2r}x_2^p + \dots \geq b_1$$



Period 1

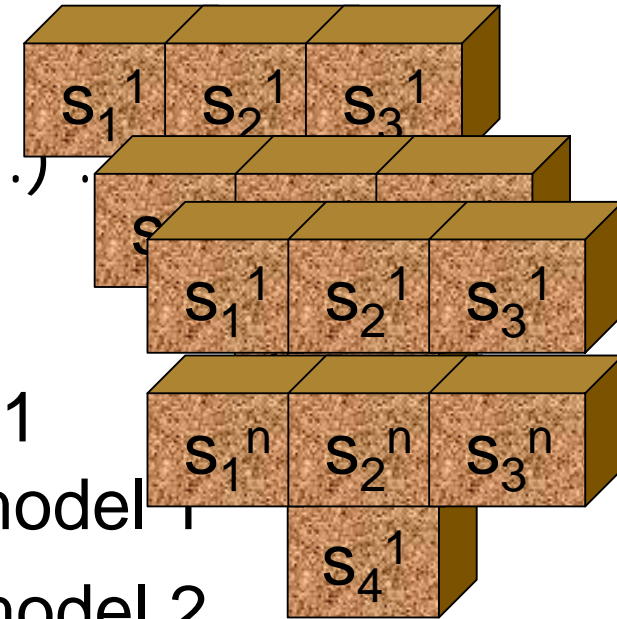
Simulated model 1

Simulated model 2

Simulated model r



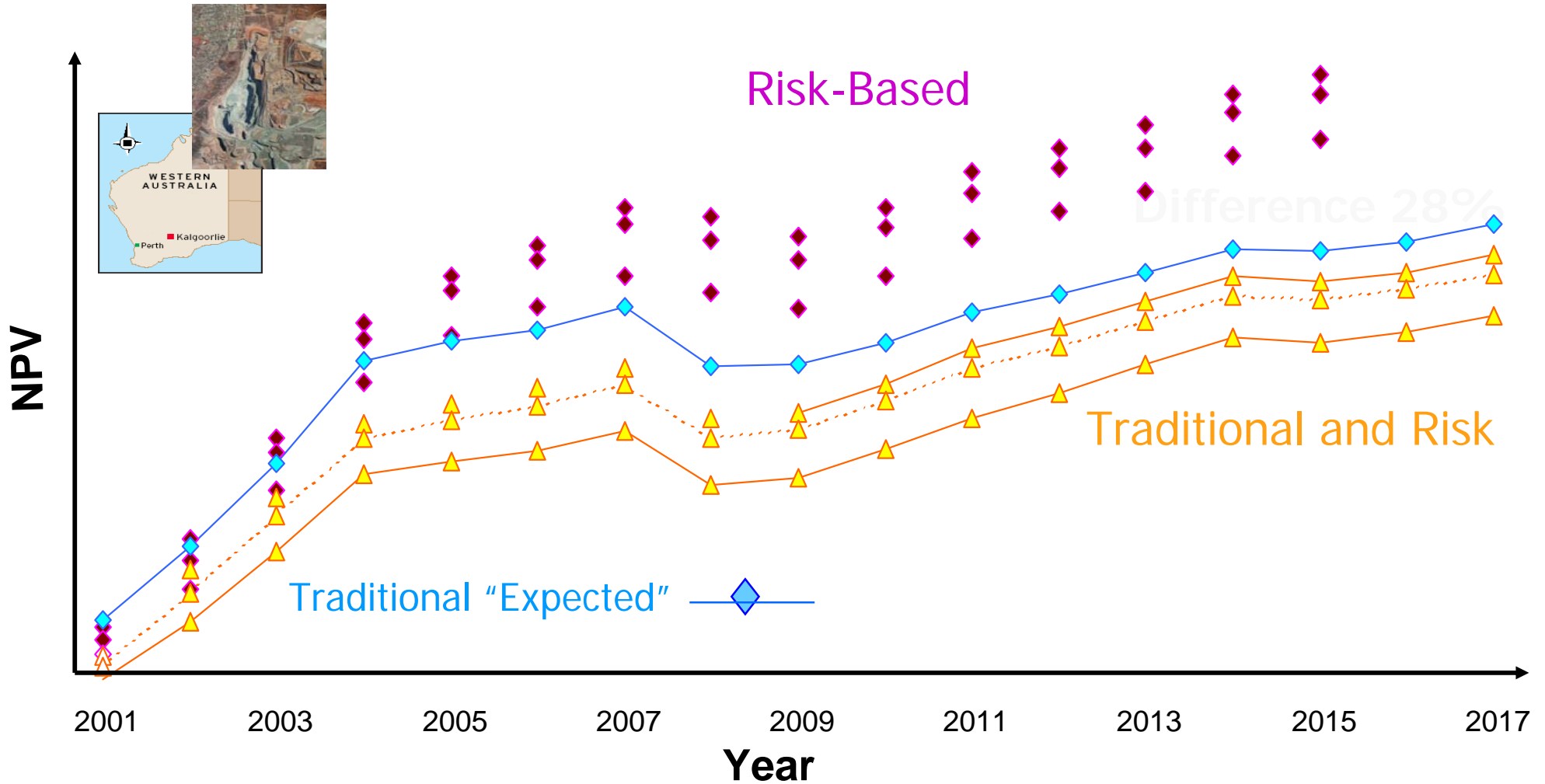
Period p



Higher NPV for Less Risk

“Uncertainty will
create opportunities and value”

Uncertainty is Good: “Base case” vs “Risk-based”



Discounting Geological Risk

The discounting goes along
with production sequencing

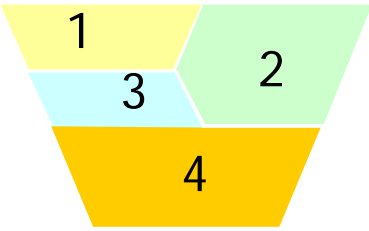
SIP - Production Scheduling Model

Objective function

$$\begin{aligned}
 \text{Max } & \sum_{t=1}^P \left[\sum_{i=1}^N E\{(\text{NPV})_i^t\} b_i^t \right. && \longrightarrow \text{Part 1} \\
 & \text{Mill \& dump} \\
 & - \sum_{s=1}^M (c_u^{ty} d_{su}^{ty} + c_l^{ty} d_{sl}^{ty}) && \longrightarrow \text{Part 2} \\
 & \text{Risk management} \\
 & - \sum_{i=1}^U E\{(\text{NPV})_i^t + \text{MC}_i^t\} * S_i^t && \longrightarrow \text{Part 3} \\
 & \text{Stockpile input} \\
 & + \sum_{s=1}^M (\text{SV})_s^t (P) q_s^t && \longrightarrow \text{Part 4} \\
 & \text{Stockpile output}
 \end{aligned}$$

Stochastic Integer Programming - SIP

A production schedule



Orebody Model 1

Deviation 1
Ore Grade 1 - TARGET []
Metal

Orebody Model 2

Deviation 2
Ore Grade 2 - TARGET []
Metal

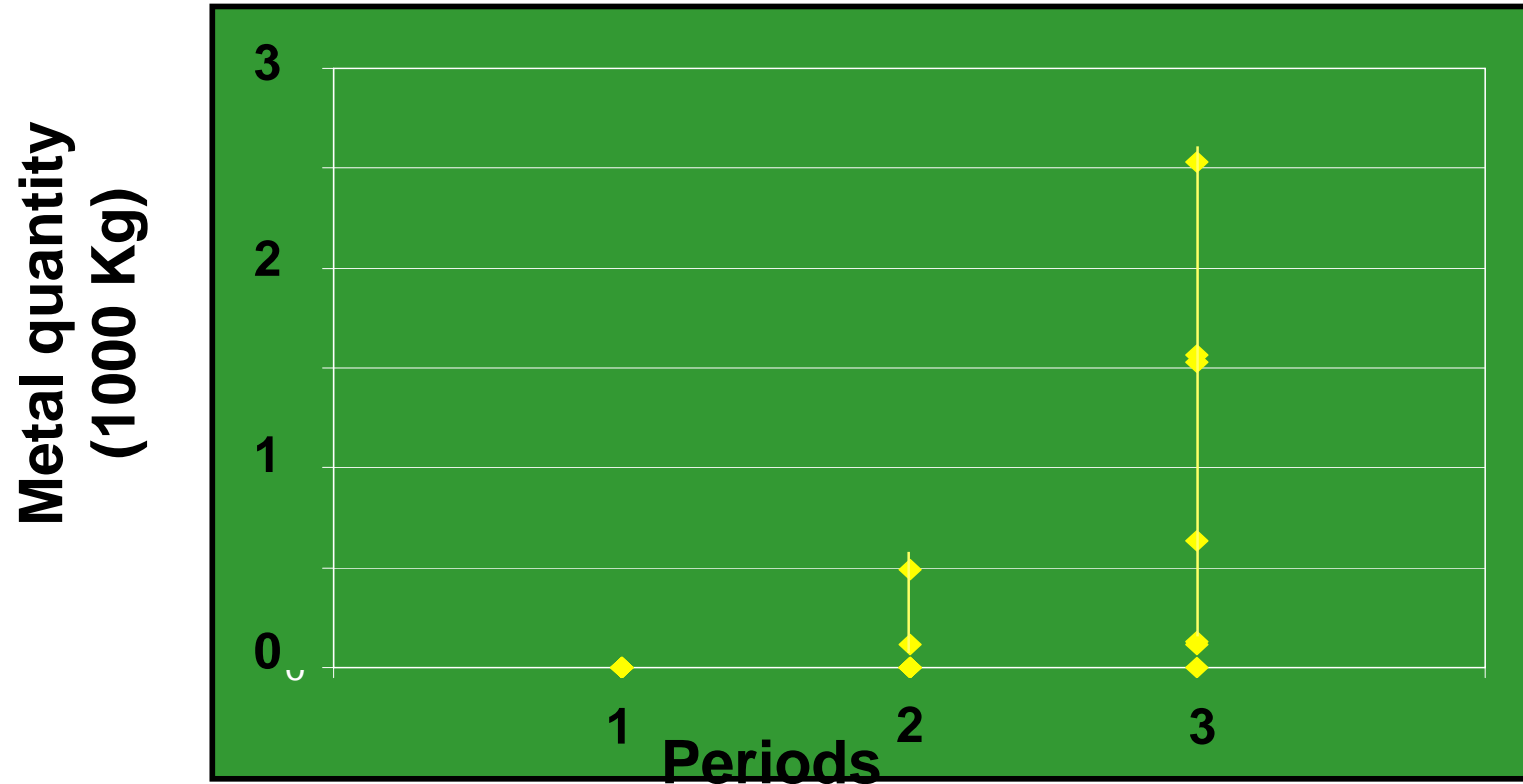
⋮

Orebody Model R

Deviation R
Ore Grade R - TARGET []
Metal

Managing Risk Between Periods

Deviations from metal production target



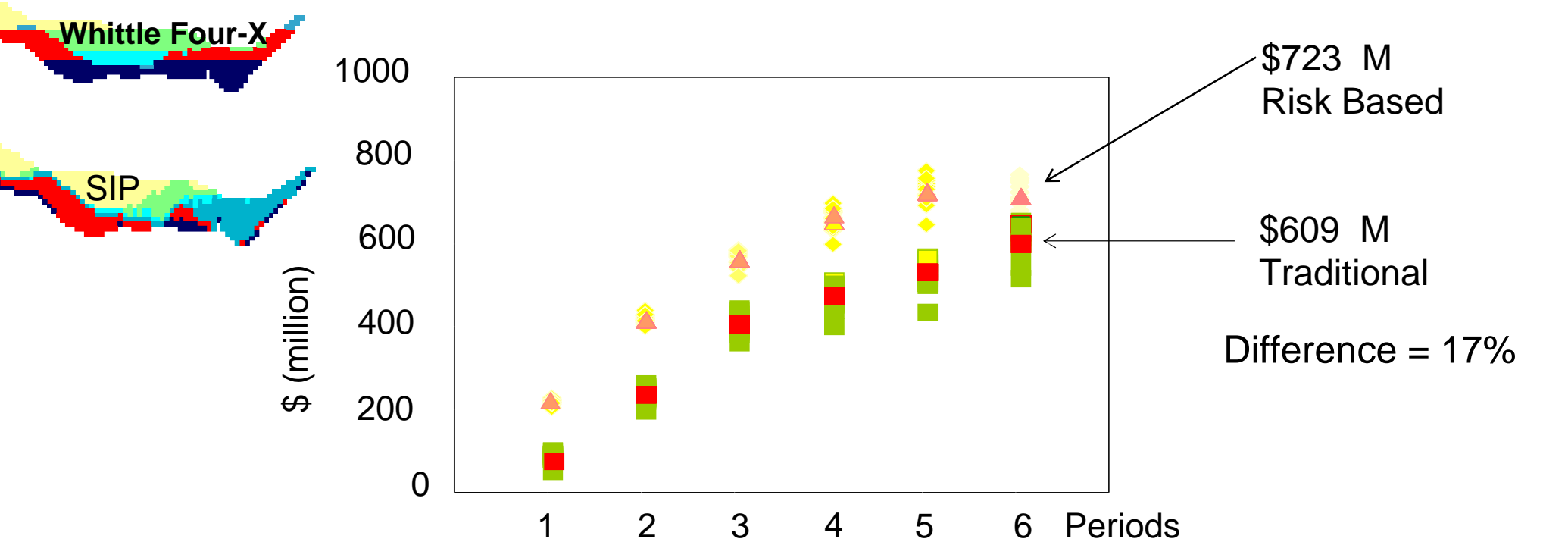
$$C_t = C^{t-1} * RDF_{t-1}$$

$$RDF_t = 1 / (1+r)^t$$

RDF – risk discounting factor

r – orebody risk discount rate

Uncertainty is Good: Traditional vs Risk-Based



Cumulative NPV values

■ SIP model
 ■ WFX

Average NPV values

■ SIP model
 ■ WFX

**Geological Risk
Discounting =
20%**

Future Drilling Data

Production sequencing with
simulated grade control drilling

'Future' Grade Control Data

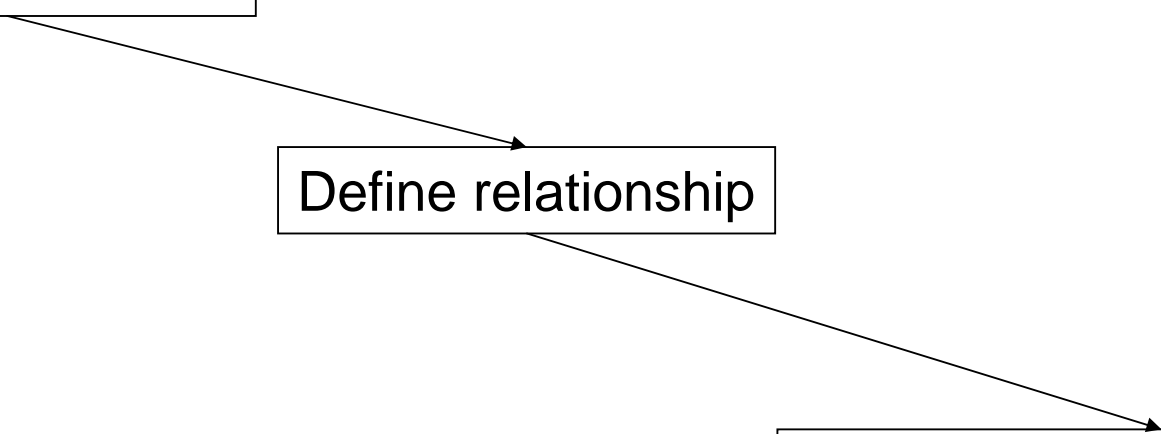
Bench/Section of pit already mined out

Exploration data
Grade control data

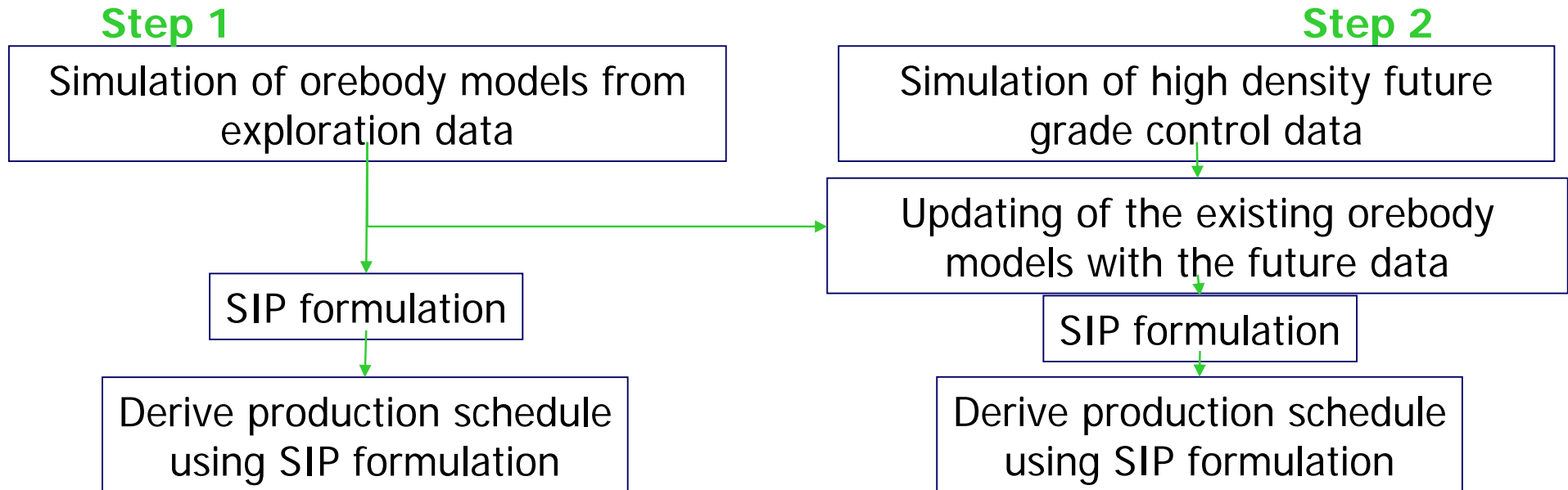
Define relationship

Exploration data
Simulate grade control data

Bench/Section of pit NOT yet mined out



Scheduling and Simulated Future Data



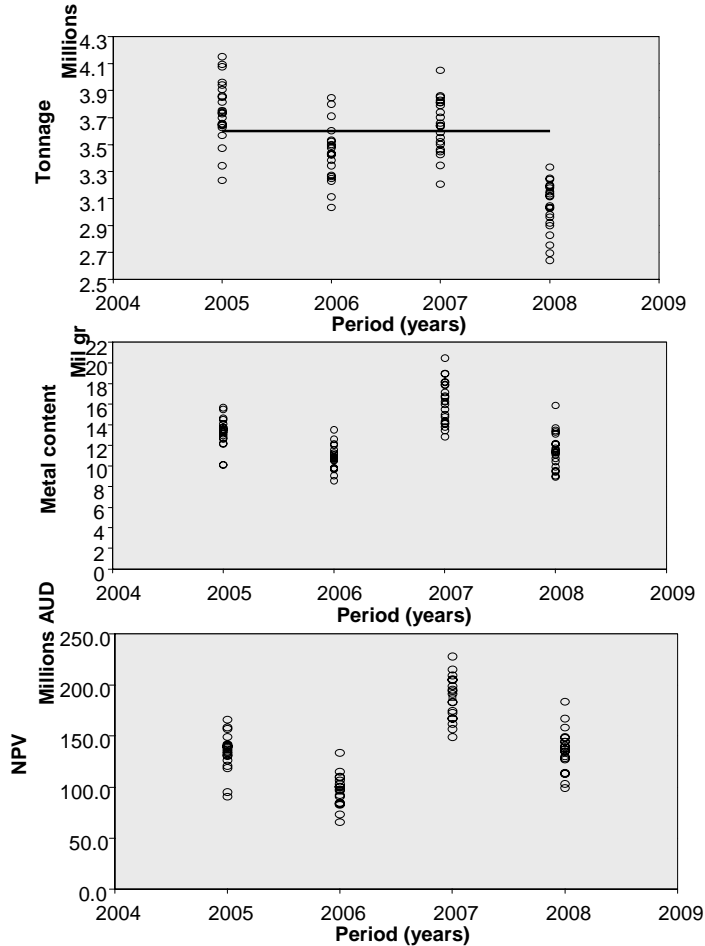
Step 3

Schedules:

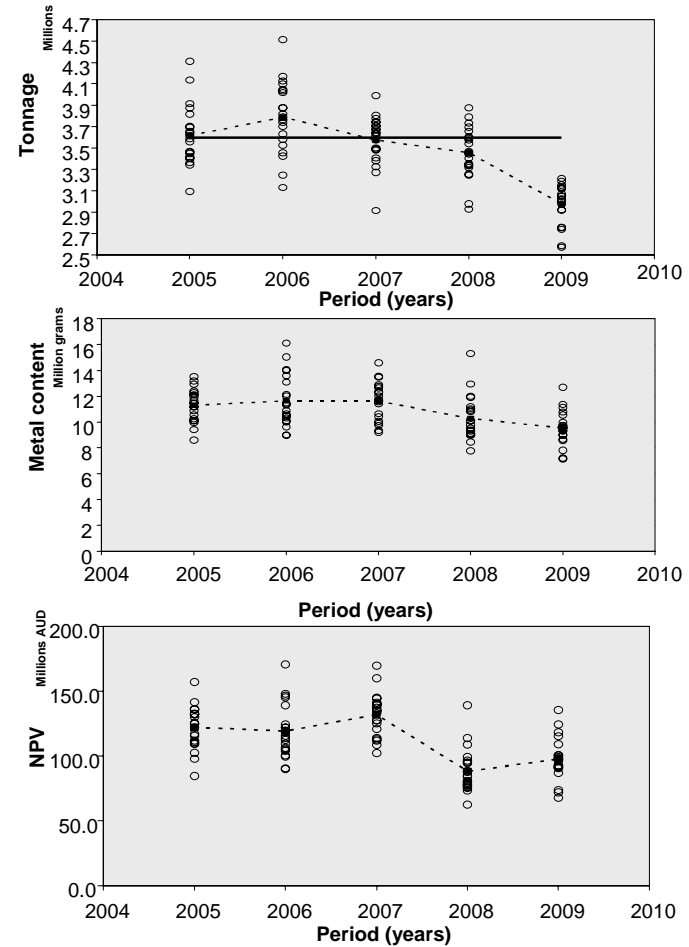
- SIP schedule derived from simulations based on exploration data
- SIP schedule derived from simulations based on simulated grade control information (updated models)
- Risk analysis of mine's schedule with the updated models

Scheduling and Simulated Future Data

SIP and Simulated Orebody



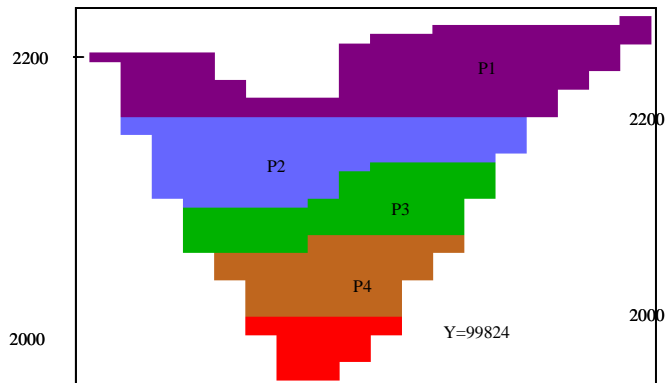
SIP and Simulated Future Data



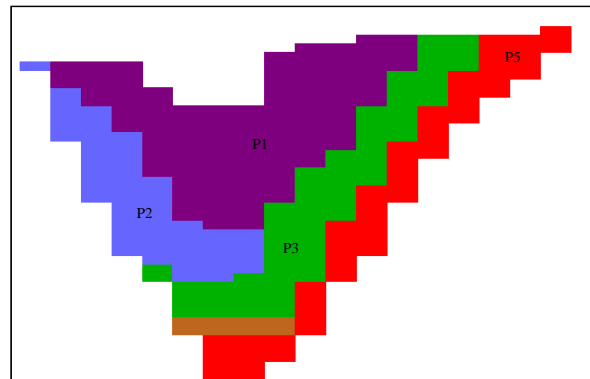
— Mill target (ore production) - - - - - Average of the simulations ○ Simulations

Scheduling and Simulated Future Data

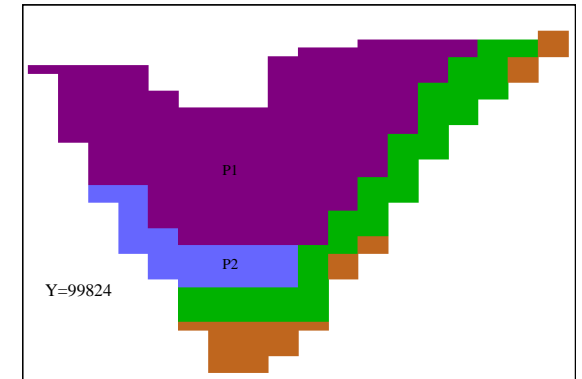
Mine's Schedule



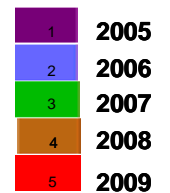
SIP & Simulated Orebody



SIP & Future data

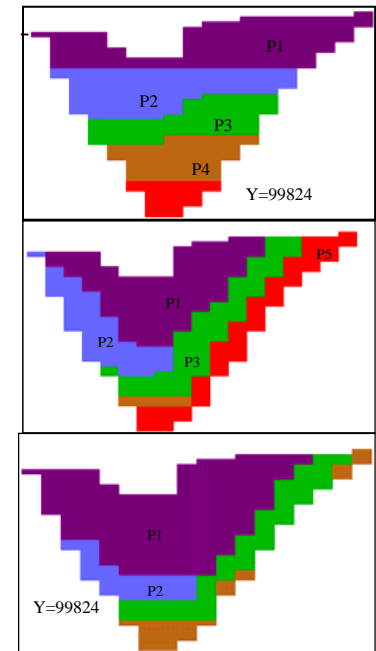


Period (years)



Scheduling and Simulated Future Data

	Simulations (exploration data)	Updated simulations (future data)	Mine's schedule (future data)
Ore Tonnes (Mt)	14	18	10
Metal Tonnes (Mt)	52	55	38
NPV (\$ Mil.)	552	560	330



Uncertainty is Great

And we will eventually find out